

# ARITHMETIC, CYCLES, MOTIVES AND ALGEBRAIC GEOMETRY

## PROGRAM

### Monday 18:

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- 9:30 - 10:30 Algebraic cycles and Hodge theory I  
James D. Lewis
- 10:45 - 11:45: Rational curves on Calabi-Yau Manifolds I  
Xi Chen
- 12:00 - 13:00 From ordinary cohomology to motivic cohomology of real varieties I  
Paulo Lima-Filho
- 16:00 - 17:00 Algebraic cycles and Hodge theory II  
James D. Lewis

### Tuesday 19:

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- 9:30 - 11:30: From ordinary cohomology to motivic cohomology of real varieties II  
Paulo Lima-Filho
- 10:45 - 11:45 Algebraic cycles and Hodge theory III  
James D. Lewis
- 12:00 - 13:00 Heights, rational points on varieties over function fields, and derivations I  
Henri Gillet
- 16:00 - 17:00 Heights, rational points on varieties over function fields, and derivations II  
Henri Gillet

### Wednesday 20:

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- 9:30 - 10:30 Rational curves on Calabi-Yau Manifolds II  
Xi Chen
- 10:45 - 11:45 Rational curves on Calabi-Yau Manifolds III  
Xi Chen
- 12:00 - 13:00 Heights, rational points on varieties over function fields, and derivations III  
Henri Gillet
- 16:00 - 17:00 From ordinary cohomology to motivic cohomology of real varieties III  
Paulo Lima-Filho

### Thursday 21:

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- 9:30 - 10:30: A study of mirror symmetry through log mixed Hodge theory I  
Sampei Usui
- 10:45 - 11:45 Chow motives (with integral coefficients), Rost nilpotence  
and applications I  
Stefan Gille
- 12:00 - 13:00 A crystalline criterion for good reduction on semistable K3-surfaces  
over a p-adic field  
Rogelio Pérez Buendía
- 16:00 - 17:00 Voevodsky motivic complexes and regulators  
Paulo Lima-Filho

**Friday 22:**

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|---------------|---|
| 9:30 - 11:30: | A study of mirror symmetry through log mixed Hodge theory II<br>Sampei Usui                       |
| 10:45 - 11:45 | Chow motives (with integral coefficients), Rost nilpotence<br>and applications II<br>Stefan Gille |
| 12:00 - 13:00 | Naive boundary strata and nilpotent orbits<br>Matt Kerr   |
| 16:00 - 17:00 | A non-trivial cycle on the generic abelian fourfold<br>Rusell Aaron Quiñones Estrella             |

**Saturday 23:**

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| 9:30 - 11:30: | A study of mirror symmetry through log mixed Hodge theory III<br>Sampei Usui  |
| 10:45 - 11:45 | The motivic Zeta function<br>Carlos Pompeyo-Gutiérrez   |
| 12:00 - 13:00 | A (very) special case of Bombieri-Lang for varieties over a function<br>field of characteristic $p$<br>Henri Gillet |

## Abstracts

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Title: Rational curves on Calabi-Yau manifolds

Speaker: Xi Chen

Mini course

Abstract: Calabi-Yau manifolds are complex manifolds with trivial canonical bundles similar to abelian varieties. But unlike abelian varieties, they contain rational curves. These rational curves play important roles in many problems. In these lectures, I'll talk about the existence of rational curves and their application to some Hodge theoretical problems on CY manifolds.

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Title: "Heights, rational points on varieties over function fields, and derivations"

Speaker: Henri Gillet

Mini course and lecture

Abstract: The the course will be a basic introduction to the Mordell conjecture (including Grauert's proof in the function fields case), and the Bombieri-Lang conjecture for varieties over function fields in both characteristic zero, and characteristic  $p > 0$ . In the talk I will report on some recent work on the characterisitic  $p > 0$  case.

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Title: Algebraic Cycles and Hodge Theory, I, II and III

Speaker: James D. Lewis

Mini course

Abstract: The goal of these lectures is to explain some recent work on the Beilinson-Hodge conjecture, and the impact of the Bloch-Kato theorem on this subject. The first two lectures will mostly cover background material (mixed Hodge structures, Milnor sheaves, algebraic de Rham cohomology, Deligne(-Beilinson) cohomology, Beilinson rigidity, absolute Hodge classes), followed by new developments in Lecture III.

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Title: Naive boundary strata and nilpotent orbits

Speaker: Matt Kerr

Lecture

Abstract: I will discuss ongoing work with G. Pearlstein on giving a limiting Hodge-theoretic interpretation to the topological boundary strata of Mumford-Tate domains inside their compact dual, including cases where this is not possible. I'll start by explaining our previous construction of Hodge-theoretic boundary components, which is quite different and related to the Kato-Usui partial compactification story.

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Title: A non-trivial cycle on the generic abelian fourfold

Speaker: Russel Aaron Quiñones Estrada

Lecture

Abstract: In the talk we give the construction of a non-trivial element of the higher Griffiths group  $Griff^{3,2}(A^4)$  for the generic abelian fourfold  $A^4$ . Codimension 3 means “curves” in  $A^4$ , so the key idea is to use the fact that  $A^4$  can be realized as a generalized Prym variety which contains in a natural way some curve.

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Title: A study of mirror symmetry through log mixed Hodge theory

Speaker: Sampei Usui

Three lectures

Abstract: We hope to understand the Hodge theoretic aspect of mirror symmetry in the framework of the fundamental diagram of log mixed Hodge theory. This work is a first step. We give a formulation of mirror theorem for quintic threefold and its mirror as the coincidence of log period maps with specified sections under the mirror map. Since a variation of Hodge structure on a punctured disc extends over the puncture to a log Hodge structure, we can work on and over the boundary point and we can observe clearly in high-resolution the behavior of  $\mathbb{Z}$ -structure over the boundary point. This is an advantage of log Hodge theory.

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