

## MATH 319 - SEC 003, SPRING 2014. HOMEWORK 4

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**Due :** Monday, February 24.

Please show all your work and/or justify your answers.

**Section 2.6:** Determine whether each of the equations in Problems 1 through 1-4 is exact. If it is exact, find the solution

1.  $(2x + 3) + (2y - 2)y' = 0.$
2.  $(2x + 4y) + (2x - 2y)y' = 0.$
3.  $(3x^2 - 2xy + 2)dx + (6y^2 - x^2 + 3)dy = 0.$
4.  $(2xy^2 + 2y) + (2x^2y + 2x)y' = 0.$

**Section 2.6 Problem 13** Solve the given initial value problem and determine at least approximately where the solution is valid.

$$(2x - y)dx + (2y - x)dy = 0, \quad y(1) = 3.$$

**Section 2.6 Problem 20** Show that the given equation is not exact but becomes exact when multiplied by a given integrating factor. Then solve the equation.

$$\left( \frac{\sin y}{y} - 2e^{-x} \sin x \right) dx + \left( \frac{\cos y + 2e^{-x} \cos x}{y} \right) dy = 0, \quad \mu(x, y) = ye^x.$$

**Section 2.6 Problem 25** Find an integrating factor and solve the given equation

$$(3x^2y + 2xy + y^3)dx + (x^2 + y^2)dy = 0$$

**Section 2.7 Problem 3** Consider the following initial value problem

$$y' = 0.5 - t + 2y, \quad y(0) = 1.$$

- (a) Find approximate values of the solution at  $t = 0.1, 0.2, 0.3$  and  $0.4$  using the Euler's method with  $h = 0.1$ .
- (b) Repeat part (a) with  $h = 0.05$ . Compare the results with those found in (a)
- (c) Repeat part (a) with  $h = 0.025$ . Compare the results with theses fond in (a) and (b).
- (d) FInd the solution  $y = \phi(t)$  of the given problem and evaluate  $\phi(t)$  at  $t = 0.1, 0.2, 0.3$  and  $0.4$ . Compare these values with the results of (a), (b) and (c).

**Section 3.1** In each of the problems 9 through 11 find the solution of the given initial value problem. Sketch the graph of the solution and describe its behavior as  $t$  increases

9.  $y'' + y' - 2y = 0, \quad y(0) = 1, \quad y'(0) = 1.$
10.  $y'' + 4y' + 3y = 0, \quad y(0) = 2, \quad y'(0) = -1$
11.  $6y'' - 5y' + y = 0, \quad y(0) = 4, \quad y'(0) = 0$

**Section 3.1 Problem 17** Find a differential equation whose general solution is  $y = c_1e^{2t} + c_2e^{-3t}$

**Section 3.1 Problem 21** Solve the initial value problem  $y'' - y' - 2y = 0, y(0) = \alpha, y'(0) = 2$ . Then find  $\alpha$  so that the solution approaches zero as  $t \rightarrow \infty$ .

**Section 3.2** Compute the Wronskian of the following pair of functions and determine if they are linearly independent or linearly dependent on the real line:

$$f(x) = \sin^2 x, g(x) = 1 - \cos(2x)$$